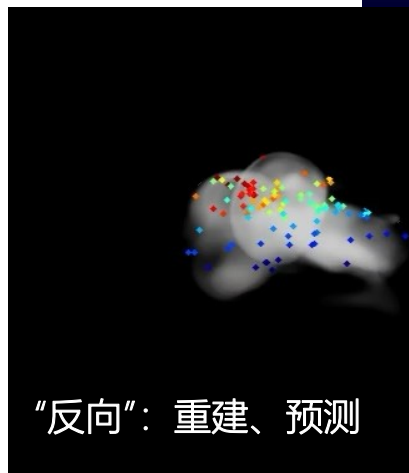
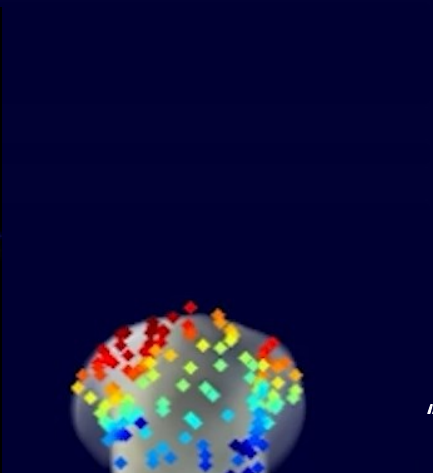


3DGS and NeRF



“反向”：重建、预测



“前向”：仿真、编辑

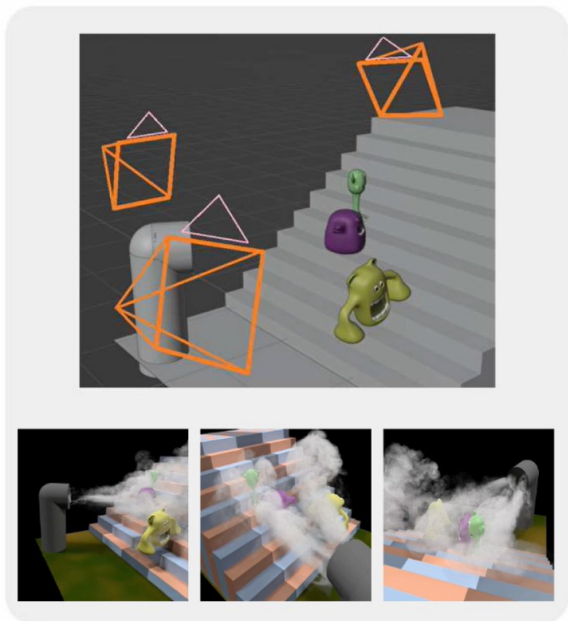
RainyGS

# Physics Simulation on New Representations like 3DGS and NeRF

## 基于新型表达的物理动态仿真及重建

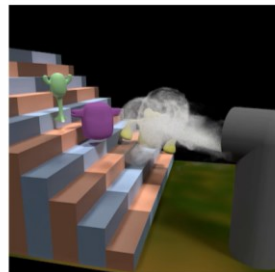
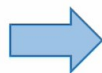
北京大学 楚梦渝

# 准确动态重建：基于神经表达的路径场重建,优化物理约束

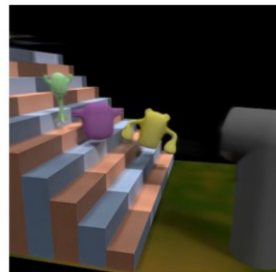


Input: Sparse-view RGB Videos

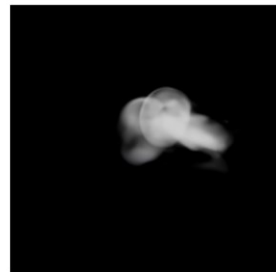
[SIGGRAPH 2024]



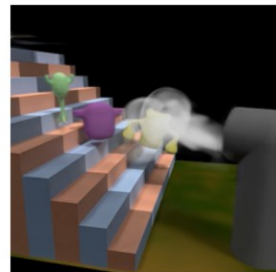
Reference



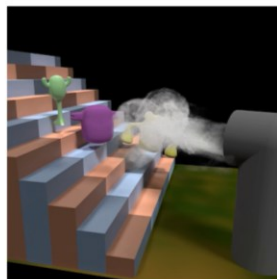
场景几何 (NeuS)  
Ours (obstacle)



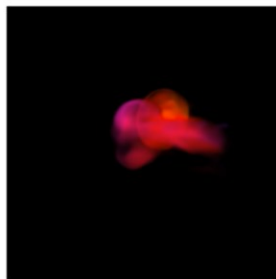
场景辐射场 (SIREN+T)  
Ours (smoke)



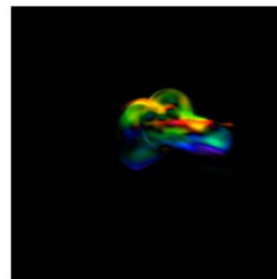
Ours (full)



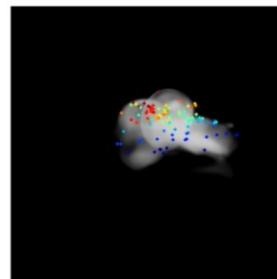
Reference



烟雾速度、涡量、路径等物理信息 (SIREN+T)  
Ours (velocity)

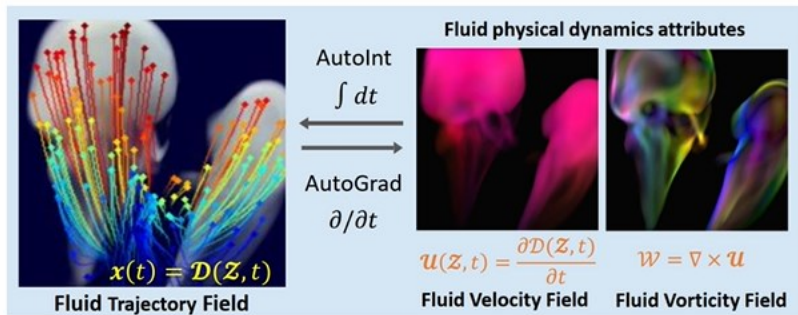


Ours (vorticity)



Ours (trajectory\*)

# 准确动态重建：基于神经表达的路径场重建,优化物理约束



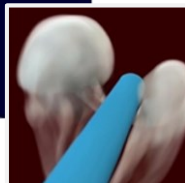
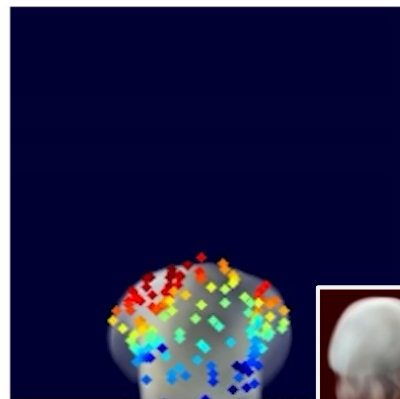
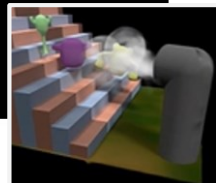
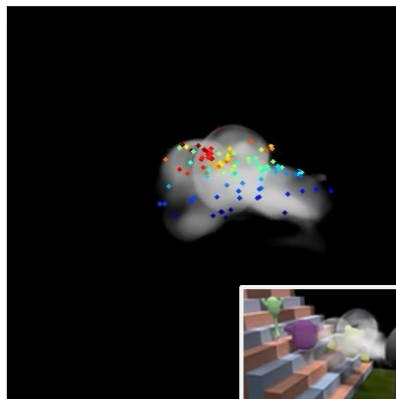
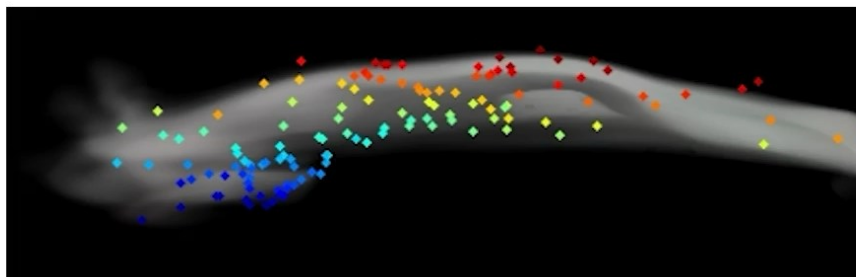
- 提出基于路径的表达:  $x(t) = D(z, t) = D(E(x, t), t)$

- 联合优化短时序的物理约束和长时序的守恒约束

短程PDE约束:  $\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} = -\frac{1}{\rho} \nabla p + \nu \nabla \cdot \nabla \mathbf{u} + \mathbf{f}$  and  $\nabla \cdot \mathbf{u} = 0$

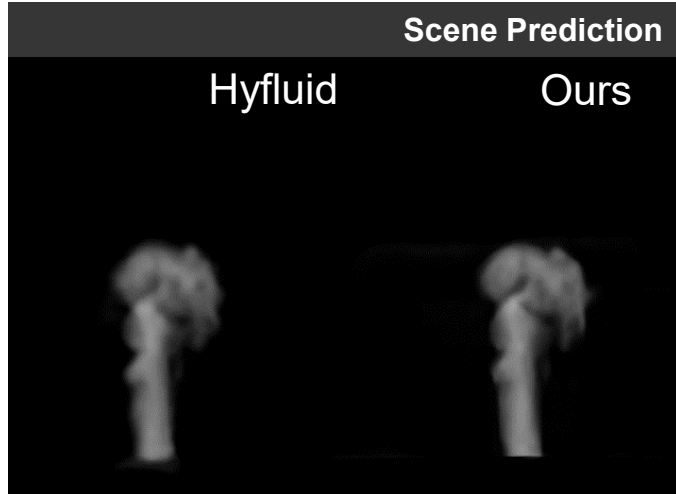
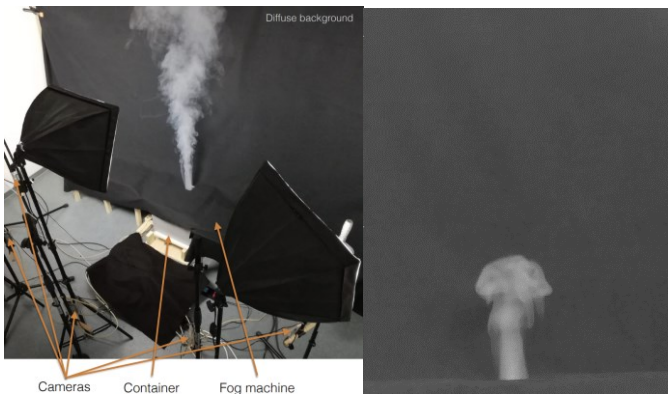
长程守恒约束:  $\mathbf{u}_a = (M_{a \rightarrow b})^T \mathbf{u}_b$  and  $M_{a \rightarrow b} = \frac{\partial \mathcal{D}(\mathcal{E}(\mathbf{x}_a, t_a), t_b)}{\partial \mathbf{x}_a}$

- 重建物理准确的动态

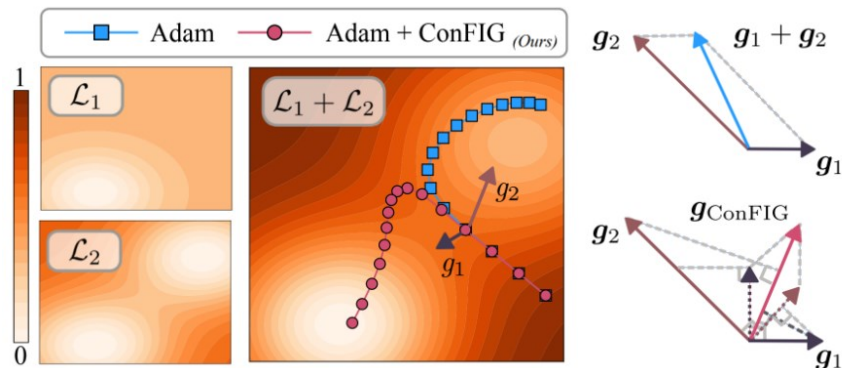


# 准确动态重建：支持动态重现和预测

- 准确重建的物理信息，可以：
  - ✓ 复现场景运动  
使用重建的速度和第一帧数据，完整重现场景动态
  - ✓ 预测未来动态  
从任意时刻的重建开始仿真，预测未来时刻动态



# 高效优化物理：提出梯度投影策略，联合优化数据和物理约束



- 联合优化 **数据 & 物理约束** 是广泛存在的难题，典型例子：PINN常因梯度冲突难以高效收敛
- ConFIG, 无冲突逆梯度方法(Conflict-Free Inverse Gradients), 具备特性:

$$\mathbf{g}_u = \mathcal{U} \left[ [\mathcal{U}(\mathbf{g}_1), \mathcal{U}(\mathbf{g}_2), \dots, \mathcal{U}(\mathbf{g}_m)] \overset{1}{-^\top} \overset{2}{\mathbf{1}_m} \right],$$

①

① 最终更新梯度  $\mathbf{g}_{\text{ConFIG}}$  与所有损失项的优化梯度**均不冲突**。

② 每个特定损失的梯度投影均匀，确保所有损失项以**相同速率优化**。

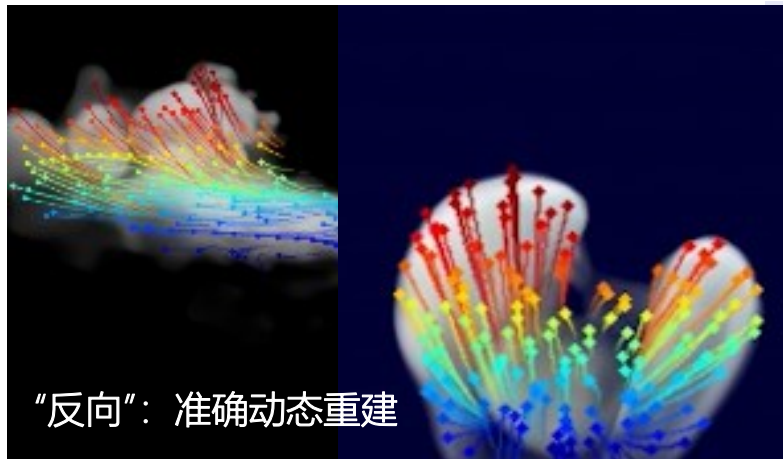
③

③  $\mathbf{g}_{\text{ConFIG}}$  步长可以根据损失项之间的冲突程度**自适应调整**。

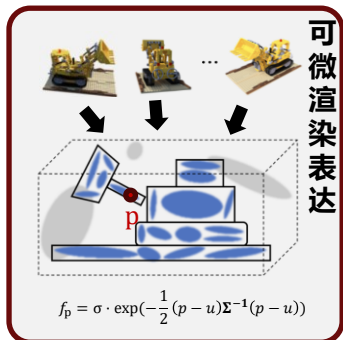
④

④ ConFIG 还介绍了更高效的**基于动量的优化**模式。

# 基于新型表达的物理动态仿真及重建



“反向”：准确动态重建



可微渲染表达

3DGS and NeRF



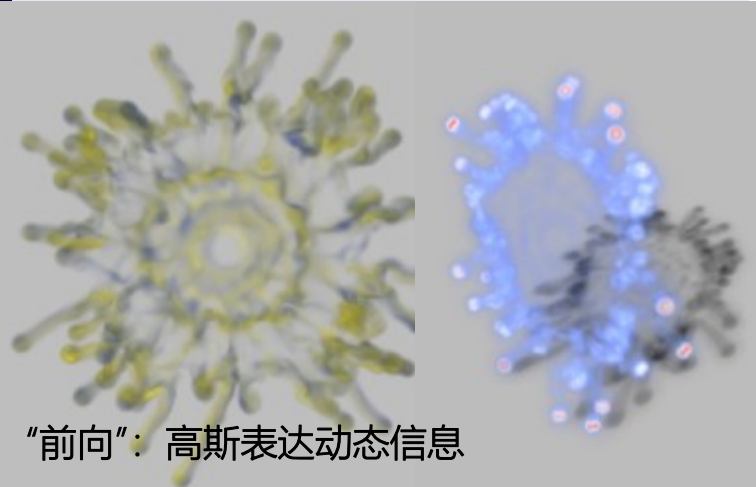
“前向”：高斯表达几何信息

RainyGS

$$\mathbf{g}_u = \mathcal{U} \left[ [\mathcal{U}(\mathbf{g}_1), \mathcal{U}(\mathbf{g}_2), \dots, \mathcal{U}(\mathbf{g}_m)] \begin{matrix} \boxed{-\top} & \boxed{\mathbf{1}_m} \\ \textcircled{1} & \textcircled{2} \end{matrix} \right],$$

$$\mathbf{g}_{\text{ConFIG}} = \mathcal{G}(\mathbf{g}_1, \mathbf{g}_2, \dots, \mathbf{g}_m) := \left( \sum_{i=1}^m \mathbf{g}_i^\top \mathbf{g}_u \right) \mathbf{g}_u \cdot \textcircled{3}$$

“反向”：高效优化物理



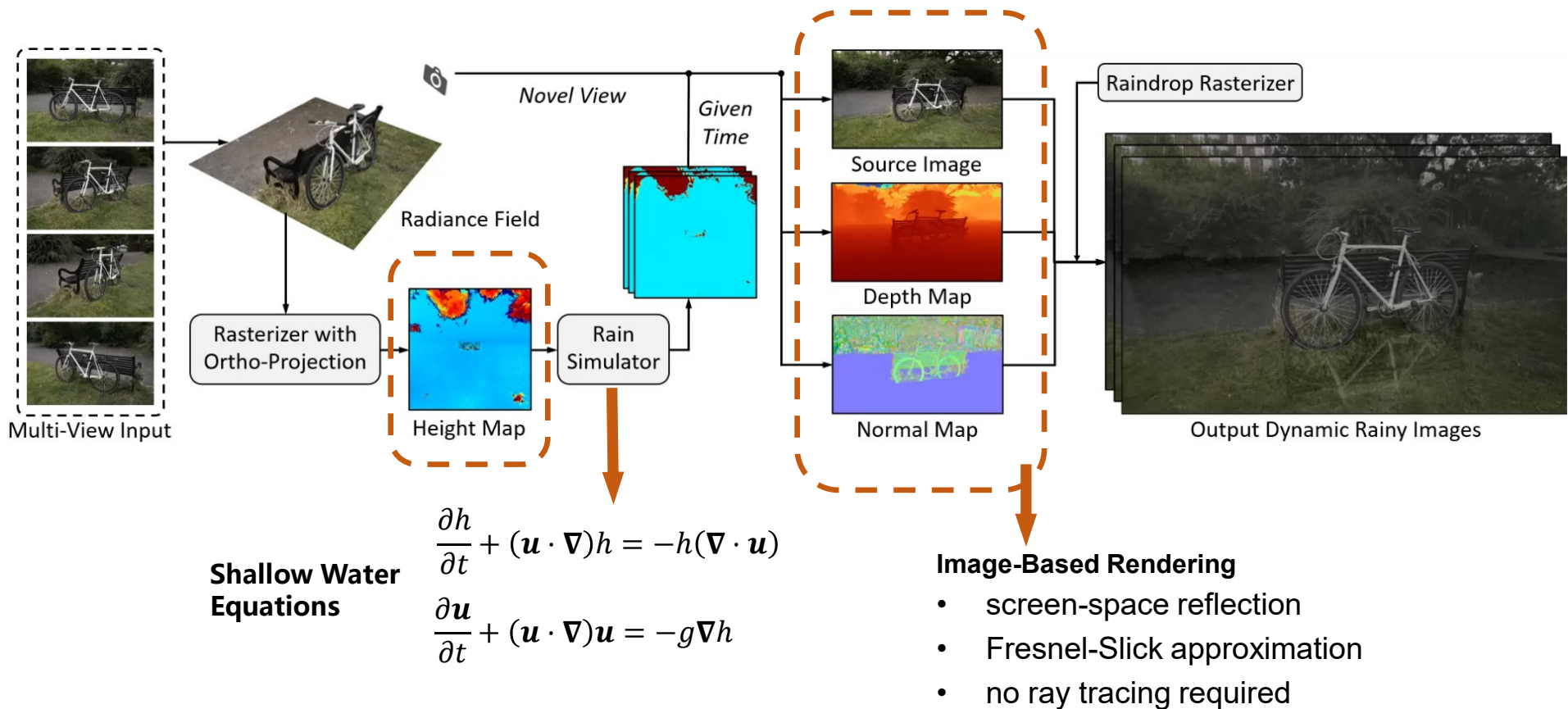
“前向”：高斯表达动态信息

# 高效动态仿真：RainyGS 孪生场景的实时降雨呈现



Multi-View Input

# 高效动态仿真：RainyGS 孪生场景的实时降雨呈现



# 高效动态仿真：RainyGS 孪生场景的实时降雨呈现

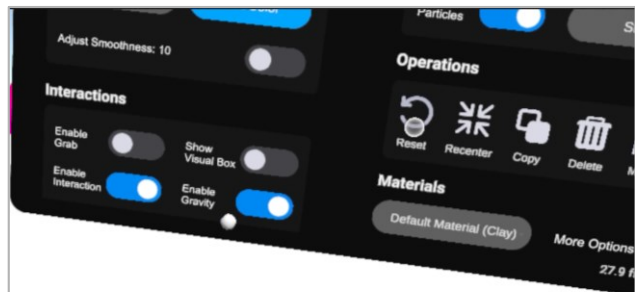
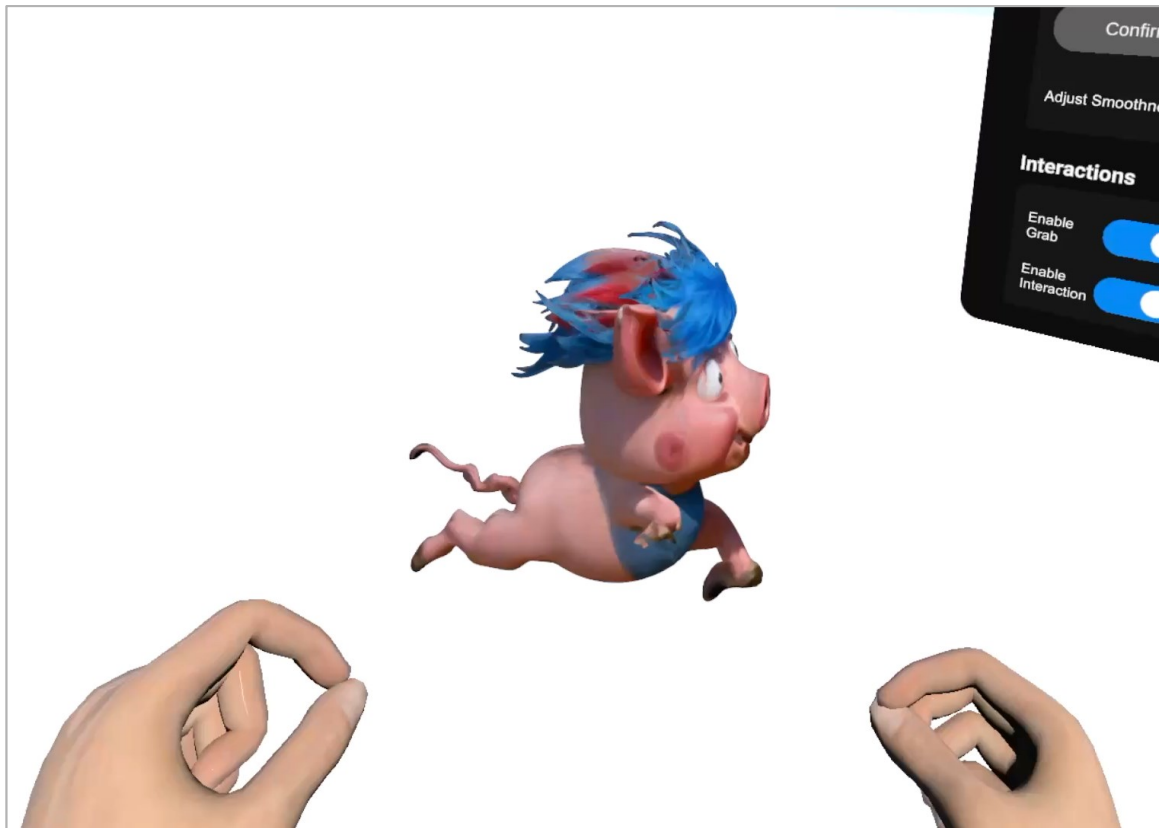
Free View Synthesis



# 高效动态仿真：RainyGS 孪生场景的实时降雨呈现



# 高效动态仿真：孪生物体的实时造型设计



# Gaussian Fluids: 以高斯场表达动态信息，求解物理方程



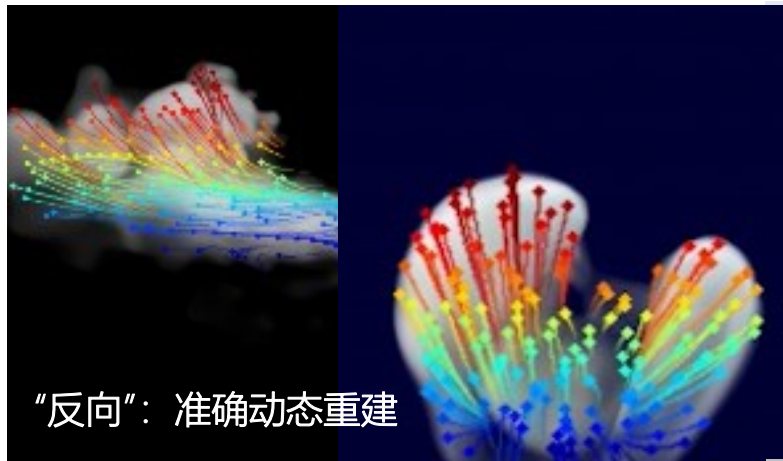
We present a grid-free fluid solver featuring a novel Gaussian representation.

- 精度具备自适应的特性
- 更好的保持流体细节、流体涡量

# Gaussian Fluids: 以高斯场表达动态信息, 求解物理方程

## 3D Leapfrog

# 总结：基于新型表达，统一前向方向仿真，统一几何动态表达

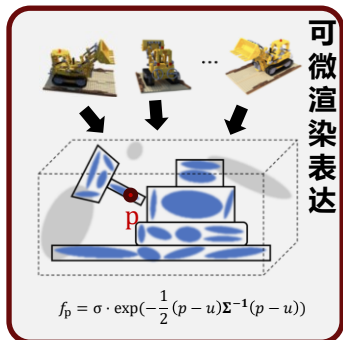


“反向”：准确动态重建

$$\mathbf{g}_u = \mathcal{U} \left[ \mathcal{U}(\mathbf{g}_1), \mathcal{U}(\mathbf{g}_2), \dots, \mathcal{U}(\mathbf{g}_m) \right] \begin{matrix} \boxed{-\top} & \boxed{\mathbf{1}_m} \\ \textcircled{1} & \textcircled{2} \end{matrix},$$

$$\mathbf{g}_{\text{ConFIG}} = \mathcal{G}(\mathbf{g}_1, \mathbf{g}_2, \dots, \mathbf{g}_m) := \left( \sum_{i=1}^m \mathbf{g}_i^\top \mathbf{g}_u \right) \mathbf{g}_u \cdot \textcircled{3}$$

“反向”：高效优化物理

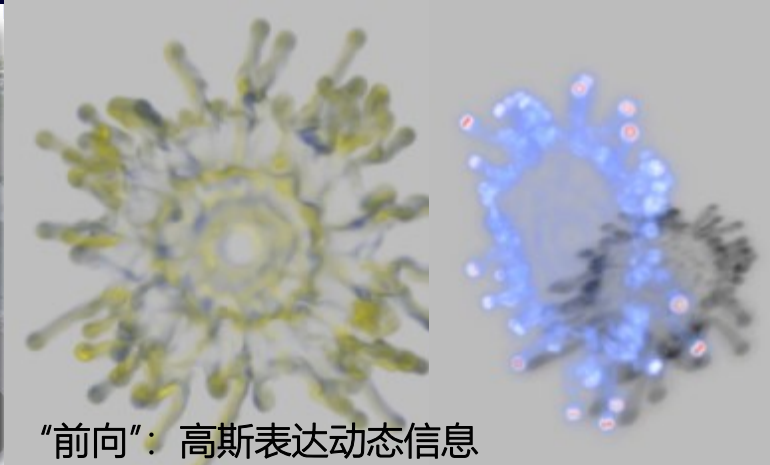


3DGS and NeRF



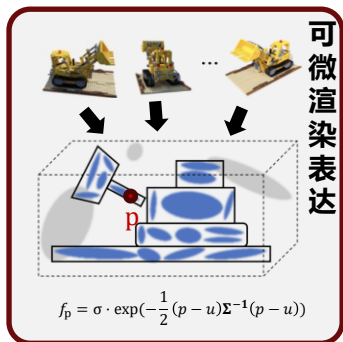
“前向”：高斯表达几何信息

RainyGS



“前向”：高斯表达动态信息

# 总结：基于新型表达，统一前向方向仿真，统一几何动态表达



$$f_p = \sigma \cdot \exp\left(-\frac{1}{2}(p - \mu)\Sigma^{-1}(p - \mu)\right)$$

3DGS and NeRF

## 新型表达:

- 统一前向、反向仿真任务
- 统一渲染、几何、和仿真
- 统一虚拟和现实，支持编辑交互

## 应用:

- 支撑真实世界仿真环境的构建
- 更紧密结合图象、语言信息，与大模型技术接轨
- 支撑具身智能、空间智能训练



# Thanks

楚梦渝

Visual Computing and Learning  
北京大学智能学院

[mchu@pku.edu.cn](mailto:mchu@pku.edu.cn)

<http://rachelcmy.github.io/>

